## THERMAL EXPANSION AND PHASE TRANSITION



## Thermal Expansion

- is the tendency of matter to change in volume in response to a change in temperature
- in expansion, there is a change in the average separation between the atoms in the object
- every linear dimension increases by the same percentage with an increase in temperature


## Average Coefficient of Linear Expansion

$$
\alpha=\frac{\Delta L / L_{i}}{\Delta T}
$$

$L_{i} \Rightarrow$ initial length
$L_{f} \Rightarrow$ final length
$\Delta L \Rightarrow L_{f}-L_{i}$
$\alpha \Rightarrow$ coefficient of linear expansion


Thermal expansion of a homogeneous metal washer. As the washer is heated, all dimensions increase. (The expansion is exaggerated in this figure.)

## Average Coefficient of Volume Expansion

$$
\beta=\frac{\Delta V / V_{i}}{\Delta T}
$$

$V_{i} \Rightarrow$ initial volume
$V_{f} \Rightarrow$ final volume
$\Delta V \Rightarrow V_{f}-V_{i}$
$\beta \Rightarrow$ coefficient of volume expansion
How about water? How does it behave?



How the density of water at atmospheric pressure changes with temperature.

## TABLE 19.2 Average Expansion Coefficients for Some Materials Near Room Temperature

|  | Average <br> Linear Expansion <br> Coefficient $(\boldsymbol{\alpha})$ <br> $\left({ }^{\circ} \mathbf{C}\right)^{-\mathbf{1}}$ | Material | Average <br> Volume Expansion <br> Coefficient $(\boldsymbol{\beta})$ <br> $\left({ }^{\circ} \mathbf{C}\right)^{\mathbf{- 1}}$ |
| :--- | :---: | :--- | ---: |
| Material | $24 \times 10^{-6}$ | Alcohol, ethyl | $1.12 \times 10^{-4}$ |
| Aluminum | $19 \times 10^{-6}$ | Benzene | $1.24 \times 10^{-4}$ |
| Brass and bronze | $17 \times 10^{-6}$ | Acetone | $1.5 \times 10^{-4}$ |
| Copper | $9 \times 10^{-6}$ | Glycerin | $4.85 \times 10^{-4}$ |
| Glass (ordinary) | $3.2 \times 10^{-6}$ | Mercury | $1.82 \times 10^{-4}$ |
| Glass (Pyrex) | $29 \times 10^{-6}$ | Turpentine | $9.0 \times 10^{-4}$ |
| Lead | $11 \times 10^{-6}$ | Gasoline | $9.6 \times 10^{-4}$ |
| Steel | $0.9 \times 10^{-6}$ | Air at $0^{\circ} \mathrm{C}$ | $3.67 \times 10^{-3}$ |
| Invar (Ni-Fe alloy) | $12 \times 10^{-6}$ | Helium | $3.665 \times 10^{-3}$ |
| Concrete |  |  |  |

## Exercises

- A steel girder is 200 m long at $20^{\circ} \mathrm{C}$. If the extremes of temperature to which it might be exposed are $-30^{\circ} \mathrm{C}$ to $+40^{\circ} \mathrm{C}$, how much will it contract and expand?
- Rubber has a negative average coefficient of linear expansion. What happens to the size of a piece of rubber as it is warmed?


## Exercises

- A certain glass rod is 30.0 cm long by 1.50 cm in diameter. If the temperature of the rod increases by $65^{\circ} \mathrm{C}$, what is the increase in (a) its length, (b) its diameter, and (c) its volume? (Assume that $\alpha=9.00 \times$

- It is shown that $3 \boldsymbol{\alpha}=\beta$, now show that the change in area of a rectangular plate is given by

$$
\Delta A=2 \alpha A_{i} \Delta T
$$

## Latent Heat ( $L$ )

- is the amount of energy released or absorbed by a chemical substance during a change of state or a phase transition

$$
L \equiv \frac{Q}{m}
$$

$L \Rightarrow$ latent heat
$Q \Rightarrow$ heat
$\mathrm{m} \Rightarrow \mathrm{mass}$

During phase change, the amount of energy transferred depends on the amount of substance involved

## Heat transfer in a phase change

- heat entering the substance - (+)
- heat leaving the substance - (-)

$$
Q= \pm m L
$$

- note: both $L_{v}$ and the boiling temperature of a material depend on pressure

The boiling point of water changes with altitude.

- As you go higher, the boiling temperature decreases.
- At sea level, the boiling point of water is $212^{\circ} \mathrm{F}(100$ ${ }^{\circ} \mathrm{C}$ ).
- As a general rule, the boiling point temperature decreases by I $\mathbf{F}^{\circ}$ for every 540 feet of altitude ( $0.56 \mathrm{C}^{\circ}$ for every 165 meters)
- there is less atmospheric pressure on the surface of liquids


## TABLE 20.2 Latent Heats of Fusion and Vaporization

| Substance | Melting <br> Point <br> $\left({ }^{\circ} \mathbf{C}\right)$ | Latent Heat <br> of Fusion <br> $(\mathbf{J} / \mathbf{k g})$ | Boiling <br> Point <br> $\left({ }^{\circ} \mathbf{C}\right)$ | Latent Heat of <br> Vaporization <br> $(\mathbf{J} / \mathbf{k g})$ |
| :--- | :---: | :---: | :---: | :---: |
| Helium | -269.65 | $5.23 \times 10^{3}$ | -268.93 | $2.09 \times 10^{4}$ |
| Nitrogen | -209.97 | $2.55 \times 10^{4}$ | -195.81 | $2.01 \times 10^{5}$ |
| Oxygen | -218.79 | $1.38 \times 10^{4}$ | -182.97 | $2.13 \times 10^{5}$ |
| thyl alcohol | -114 | $1.04 \times 10^{5}$ | 78 | $8.54 \times 10^{5}$ |
| Water | 0.00 | $3.33 \times 10^{5}$ | 100.00 | $2.26 \times 10^{6}$ |
| Sulfur | 119 | $3.81 \times 10^{4}$ | 444.60 | $3.26 \times 10^{5}$ |
| Lead | 327.3 | $2.45 \times 10^{4}$ | 1750 | $8.70 \times 10^{5}$ |
| Aluminum | 660 | $3.97 \times 10^{5}$ | 2450 | $1.14 \times 10^{7}$ |
| Silver | 960.80 | $8.82 \times 10^{4}$ | 2193 | $2.33 \times 10^{6}$ |
| Gold | 1063.00 | $6.44 \times 10^{4}$ | 2660 | $1.58 \times 10^{6}$ |
| Copper | 1083 | $1.34 \times 10^{5}$ | 1187 | $5.06 \times 10^{6}$ |

- latent heat of solidification = latent heat of fusion
- latent heat of vaporization $=$ latent heat of condensation


## Specific Heat (c)

- is the heat capacity per unit mass of a substance


## Heat Capacity ( ()

- is the amount of energy needed to raise the temperature of a particular sample of substance by $1{ }^{\circ} \mathrm{C}$

$$
Q=m c \Delta T \quad Q=C \Delta T
$$

$c \Rightarrow$ heat capacity
$Q \Rightarrow$ heat
$\mathrm{m} \Rightarrow$ mass
$\Delta T \Rightarrow$ temperature change

| TABLE 20.1 | Specific Heats of Some <br> Substances at $\mathbf{2 5}^{\circ} \mathrm{C}$ and <br> Atmospheric Pressure |  |
| :--- | :---: | :---: |
|  | Specific Heat $\mathbf{c}$ |  |
|  | J/kg $\cdot{ }^{\circ} \mathbf{C}$ | cal/g $\cdot{ }^{\circ} \mathbf{C}$ |
| Substance |  |  |
| Elemental Solids | 900 | 0.215 |
| Aluminum | 1830 | 0.436 |
| Beryllium | 230 | 0.055 |
| Cadmium | 387 | 0.0924 |
| Copper | 322 | 0.077 |
| Germanium | 129 | 0.0308 |
| Gold | 448 | 0.107 |
| Iron | 128 | 0.0305 |
| Lead | 703 | 0.168 |
| Silicon | 234 | 0.056 |
| Silver |  |  |
| Other Solids | 380 | 0.092 |
| Brass | 837 | 0.200 |
| Glass | 2090 | 0.50 |
| Ice $\left(-5^{\circ} \mathrm{C}\right)$ | 860 | 0.21 |
| Marble | 1700 | 0.41 |
| Wood |  |  |
| Liquids | 2400 | 0.58 |
| Alcohol $($ ethyl $)$ | 140 | 0.033 |
| Mercury | 4186 | 1.00 |
| Water $\left(15^{\circ} \mathrm{C}\right)$ |  |  |
| Gas | 2010 | 0.48 |
| Steam $\left(100^{\circ} \mathrm{C}\right)$ |  |  |

## Phase Transition of Water

- transfer of energy (heat) doesn't result in a change in temperature


A plot of temperature versus energy added when 1.00 g of ice initially at $-30.0^{\circ} \mathrm{C}$ is converted to steam at $120.0^{\circ} \mathrm{C}$.

Chapter problem 20-66
Serway (5th ed), p. 638
A cooking vessel on a slow burner contains 10.0 kg of water and an unknown mass of ice in equilibrium at $0^{\circ} \mathrm{C}$ at time $t=0$. The temperature of the mixture is measured at various times, and the result is plotted in the figure. During the first 50.0 min , the mixture remains at $0^{\circ} \mathrm{C}$. From 50.0 min to
 60.0 min , the temperature increases to $2.00^{\circ} \mathrm{C}$. Neglecting the heat capacity of the vessel, determine the initial mass of the ice.

